

**THREE-QUANTA  
POSITRON ANNIHILATION  
IN BLOOD SAMPLES OF  
DIFFERENT OXYGENATION LEVELS**

**MARY CHIN & NICHOLAS SPYROU**

**Department of Physics, University of Surrey, Guildford GU2 7XH, UK**



**UNIVERSITY OF  
SURREY**



# THREE-QUANTA POSITRON ANNIHILATION

**1. WHY**

**2. CONTROVERSIES**

**3. HOW**

# THREE-QUANTA POSITRON ANNIHILATION

Used in material science but not  
medical imaging

Positron Emission Tomography  
(PET) currently is based on  
**TWO**-QUANTA annihilations  
only



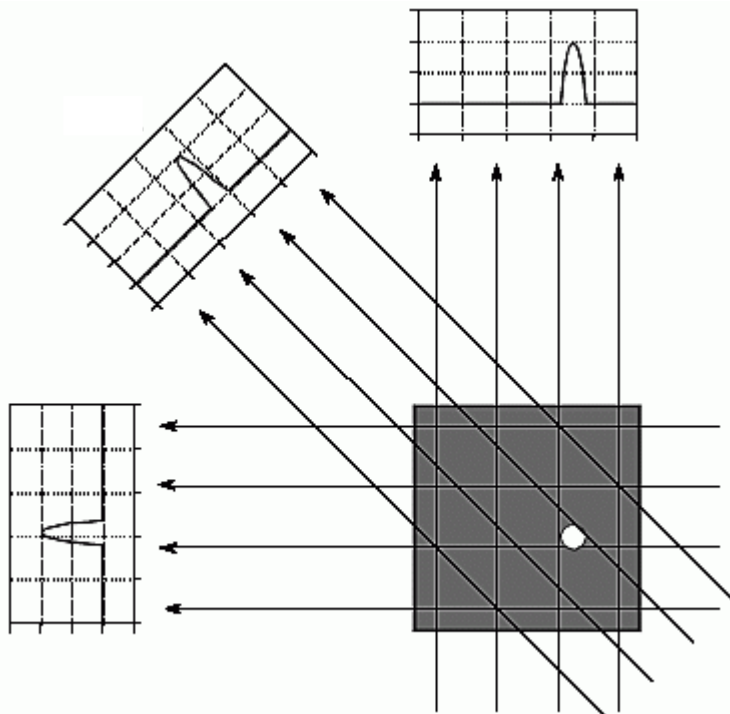
# THREE-QUANTA POSITRON ANNIHILATION

Attractions:

1. Image reconstruction without backprojection
2. Molecular imaging without dedicated radiopharmaceutical or contrast agent

# 2 $\gamma$ PET

## IMAGE RECONSTRUCTION



WE HAVE TO BACK-PROJECT  
COZ WE DON'T KNOW AT WHICH  
POINT THE ANNIHILATION  
HAPPENED

LINE OF RESPONSE

# 3 $\gamma$ PET

By conservations of  
energy & momentum

**KNOWN**

$(E_1, \alpha_1)$

$(E_2, \alpha_2)$

$(E_3, \alpha_3)$

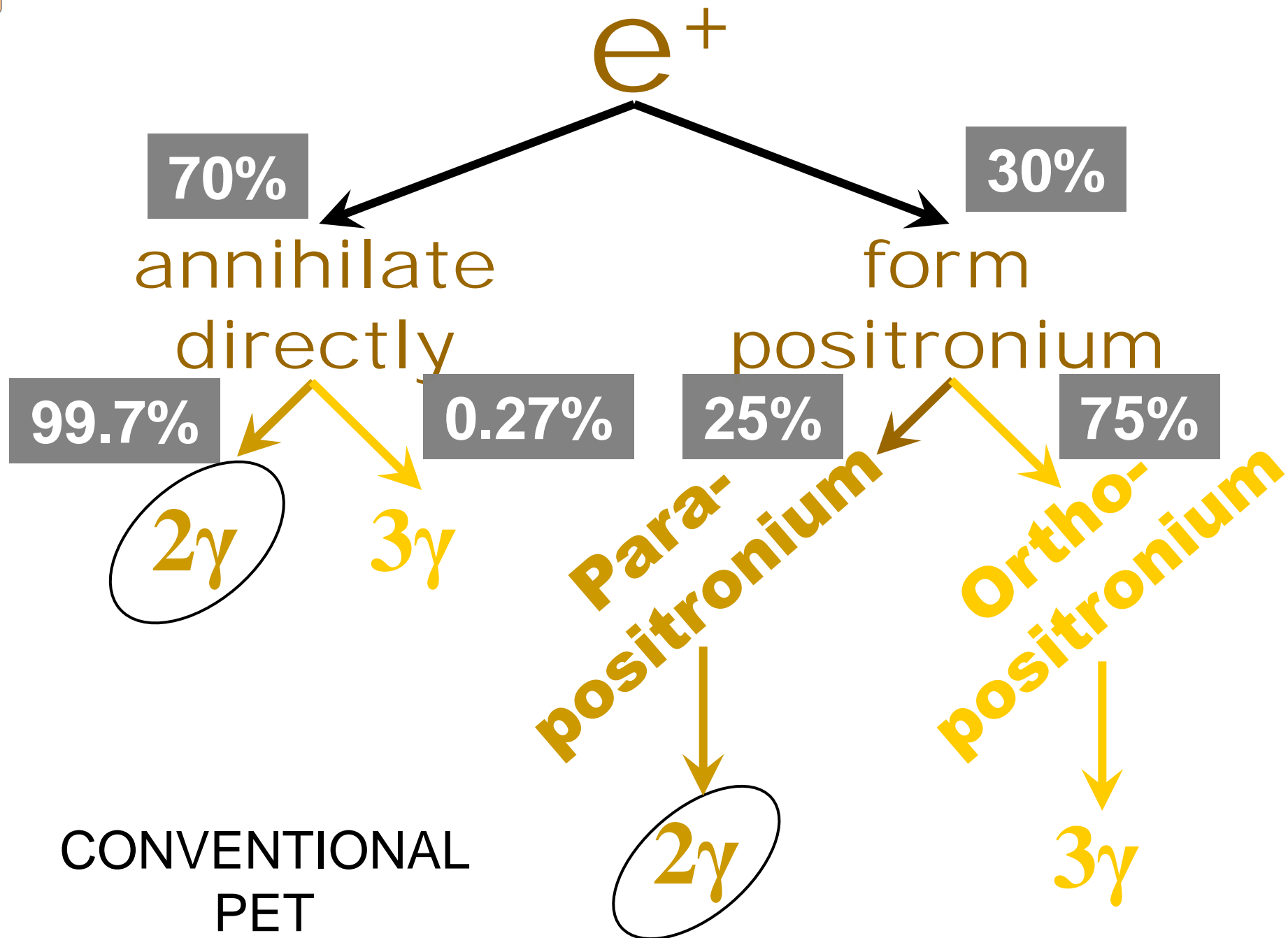
**UNKNOWNNS**

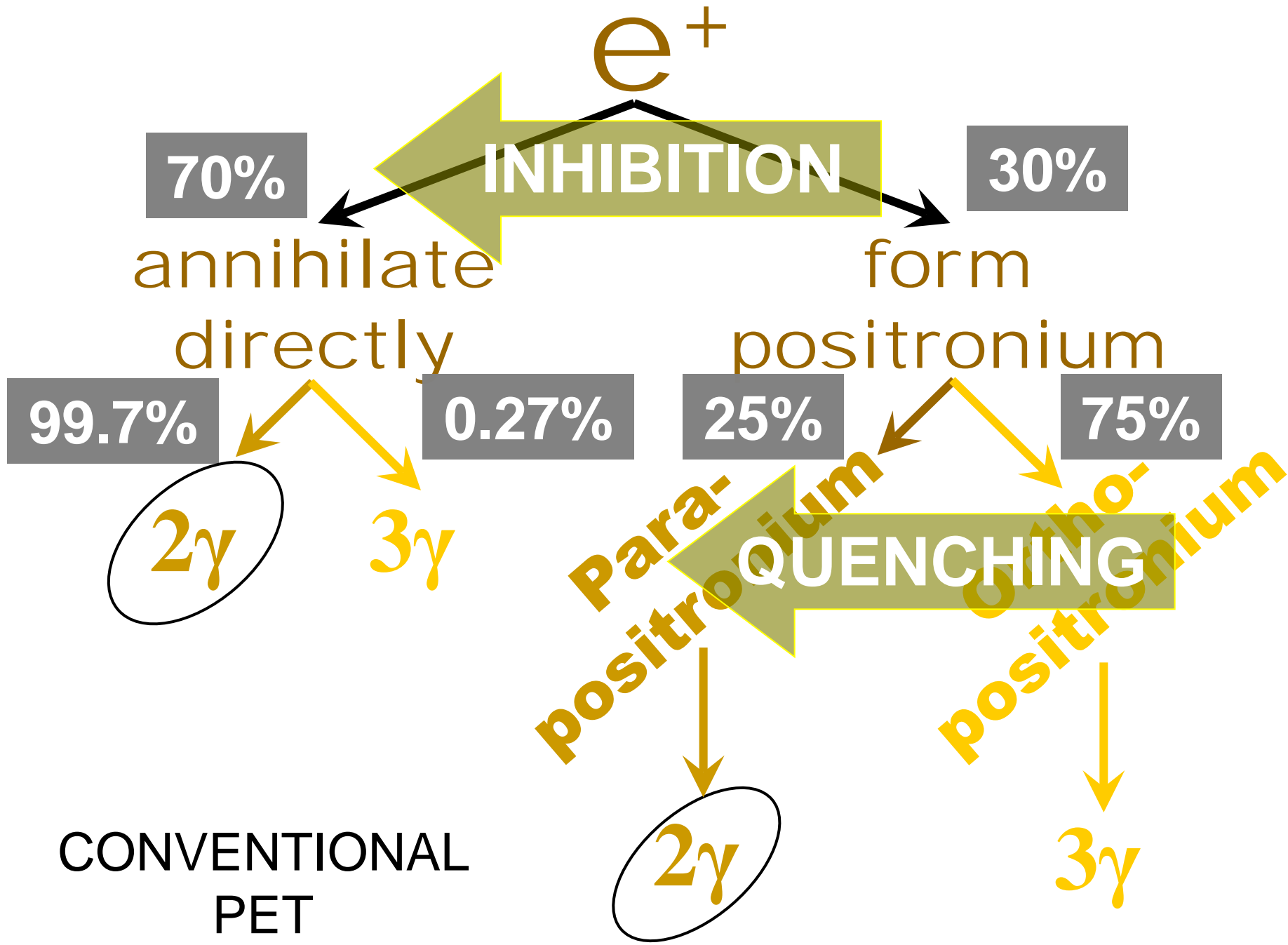
$(x_1, y_1, z_1)$



solve simultaneous eqs

POINT OF RESPONSE







**INHIBITION**

annihilate  
directly

form  
positronium

**AGENTS** eg  
 $O_2$ , NO,  $CO_2$

*oxygenation*

**Para-  
positronium**

**QUENCHING**

**Ortho-  
positronium**

# PROSPECTS FOR MOLECULAR IMAGING





MEASURE  $3\gamma/2\gamma$  YIELD



FIND OUT  $O_2$  IN BODY TISSUES?

**PROSPECTS FOR  
MOLECULAR IMAGING**

**PROPOSAL**

**Three-Gamma Annihilation Imaging in Positron  
Emission Tomography**

Krzysztof Kacperski\*, Nicholas M. Spyrou, and F. Alan Smith

*Abstract*—It is argued that positron annihilation into three photons, although quite rare, could still be used as a new imaging modality of positron emission tomography. The information gained when the three decay photons are detected is significantly higher than in the case of 511 keV two-gamma annihilation. The performance of three-gamma imaging in terms of the required detector properties, spatial resolution and counting rates is discussed. A simple proof-of-principle experiment confirms the feasibility of the new imaging method.

*Index Terms*—Positron emission tomography, three-gamma annihilation.

Three-gamma imaging is potentially more powerful than standard PET because each event bears the complete position information enabling the localization of the activity distribution without use of back-projection tomographic techniques. However, only a subfraction of the three-photon events are usable as each photon energy must be above the detection threshold and only total energy deposition events can be used, as a tight total energy window and time window ( $<5$  ns) must be applied (for typical source strengths used in imaging) to reduce the strong background from two-photon decay pile-up events. However, these conditions can be met with high-resolution semiconductor detectors as pointed out in Kacperski and Spyrou (2005), and construction of a detection system with the required attributes for such studies is not beyond the reach of current technology.

The present work answers one question raised by Kacperski and Spyrou (2005) concerning the potential biological sensitivity of the three-photon imaging. Unfortunately, one should not expect any sensitivity to the level of dissolved  $O_2$ . Our results indicate that the overall three-photon yield is about 0.5% in all samples. These conclusions assume that the direct three-photon yield is identical to that for free  $e^-$ s. Only direct measurement of the three-photon yield can determine if this assumption is correct (Seweryniak 2006).



**Table 1.** The delayed ( $F_3^{\text{de}}$ ) and total ( $F_3$ ) three-photon yields as well as the fit parameters ( $K_p$  and  $K_{\text{cap}}/\lambda_d$ ) for the various liquid samples (HSA is for human serum albumin).

Material	Oxygen	$F_3^{\text{de}}$ (%)	$F_3$ (%)	$K_p$ (ns <sup>-1</sup> )	$R = K_{\text{cap}}/\lambda_d$
Iso-octane	Low	0.58	0.85	1.34	2.15
	High	0.39	0.65	2.27	2.06
Water	Low	0.26	0.52	2.77	3.05
	High	0.25	0.51	2.84	3.07
Saline	Low	0.24	0.51	2.86	3.14
	High	0.24	0.51	2.98	3.07
HSA	Low	0.25	0.51	2.64	3.30
	High	0.25	0.51	2.95	2.96
Blood	Venous	0.25	0.52	2.86	3.02

The present work answers one question raised by Kacperski and Spyrou (2005) concerning the potential biological sensitivity of the three-photon imaging. Unfortunately, one should not expect any sensitivity to the level of dissolved O<sub>2</sub>. Our results indicate that the overall three-photon yield is about 0.5% in all samples. These conclusions assume that the direct three-photon yield is identical to that for free e<sup>-</sup>s. Only direct measurement of the three-photon yield can determine if this assumption is correct (Seweryniak 2006).

# DATA TO BE PRESENTED HERE

The GAMMASPHERE detector system when it was stationed at Argonne National Laboratory

$4\pi$  array of 110 Compton-suppressed high-purity germanium detectors (HPGe)

Experiment carried out by Dr K Kacperski when he was employed as a postdoc at the University of Surrey



source: [www.nuclear.kth.se](http://www.nuclear.kth.se)

# GAMMASPHERE: AN UNPRECEDENTED LUXURY FOR US

## LUXURY #1 NEAR-4 $\pi$ SOLID ANGLE

## LUXURY #2 MULTI-DIMENSIONAL DATA WRITTEN OUT

# GAMMASPHERE information, EVENT DATA RECORD

The EVENT DATA RECORD consists of a header and data as:

```
typedef struct event_buffer
{
    u_short RecordType;          /* 0 event data type= 3          */
    u_short RecordLength;       /* 1 number of bytes in this record */
    u_short RecordVer;         /* 2 record version or subtype    */
    u_short HeaderBytes;       /* 3 number of bytes in header    */
    u_short EffNumber;         /* 4 eff processor number         */
    u_short StreamID;          /* 5 event stream ID             */
    u_short EffSequence;       /* 6 eff sequence number         */
    u_short ModeFlags;          /* 7 event format flags          */
    u_short DataLength;        /* 8 number of i*2 data words     */
    u_short ChecksumType;      /* 9 type of checksum            */
    u_short Checksum;          /* 10 checksum value              */
    u_short EventData[EB_SIZE]; /* event data area                */
}
    EVENT_BUFFER;
```

# GAMMASPHERE: AN UNPRECEDENTED LUXURY FOR US

## LUXURY #1 NEAR-4 $\pi$ SOLID ANGLE

## LUXURY #2 MULTI-DIMENSIONAL DATA WRITTEN OUT

**GAIN CORRECTION CONTROL BIT** - EVENT PROCESSING CONTROL BITS

**DATA**

1	gcmode	gain correction on/off
2	tmmode	time veto on/off
3	hmode	adjacent detector veto on/off

**The EVENT DATA CONTROL BITS FOR EACH DETECTOR**

```
typedef struct {
    u_s 4 writeget      output ge time on/off
    u_s 5 writegef      output full ge data on/off
    u_s 6 writebgo      output of BGO data on/off
    u_s BIT - EVENT DATA CONTROL BITS FOR EACH EVENT
    u_s
    u_s 7 writeallge    output of dirty ge data on/off
    u_s 8 writeallbgo   output of clean bgo data on/off
    u_s
    u_s BIT - MISC
    u_s
    u_s 9 writeIsomerTag
    u_s 10 rf_timing    ge times calculated vs rf pulses
    u_s                 (subtract tac2 on the fly)
} EVENT_BUFFER;
```

**GAMMASPHERE: AN UNPRECEDENTED LUXURY FOR US**

**LUXURY #1 NEAR- $4\pi$  SOLID ANGLE**

**LUXURY #2 MULTI-DIMENSIONAL DATA WRITTEN OUT**



# GAMMASPHERE: AN UNPRECEDENTED LUXURY FOR US

## LUXURY #1 NEAR-4 $\pi$ SOLID ANGLE

1	hpid	bgo hit pattern	(0xfe00)	1111 1110 0000 0000	[1]
		and ge hit bit	(0x0100)	0000 0001 0000 0000	
		and id register	(0x00ff)	0000 0000 1111 1111	
2	ge_high	14 bit high res ge	(0x3fff)	0011 1111 1111 1111	
		and over-range bit	(0x4000)	0100 0000 0000 0000	
		and Pileup bit	(0x8000)	1000 0000 0000 0000	
3	ge_side	12 bit side ch ge	(0x0fff)	0000 1111 1111 1111	[2]

The appropriate mask to extract the information is shown both in hex and binary formats.

The rest of the events depend on what EFF write out options are on:

If the "writeget" [4] (germanium time) or "writegef" [5] (trap + lowres signals) are set

4	ge_time	12/13 bit	[5] ge time	(0x1fff)	0001 1111 1111 1111
---	---------	-----------	-------------	----------	---------------------

If "writegef" [5] (trap + lowres signals) is set:

5	ge_trap	12 bit trap corr	(0x0fff)	0000 1111 1111 1111
6	ge_low	12 bit low res ge	(0x0fff)	0000 1111 1111 1111

If "writebgo" [6] (clean bgo) is set:

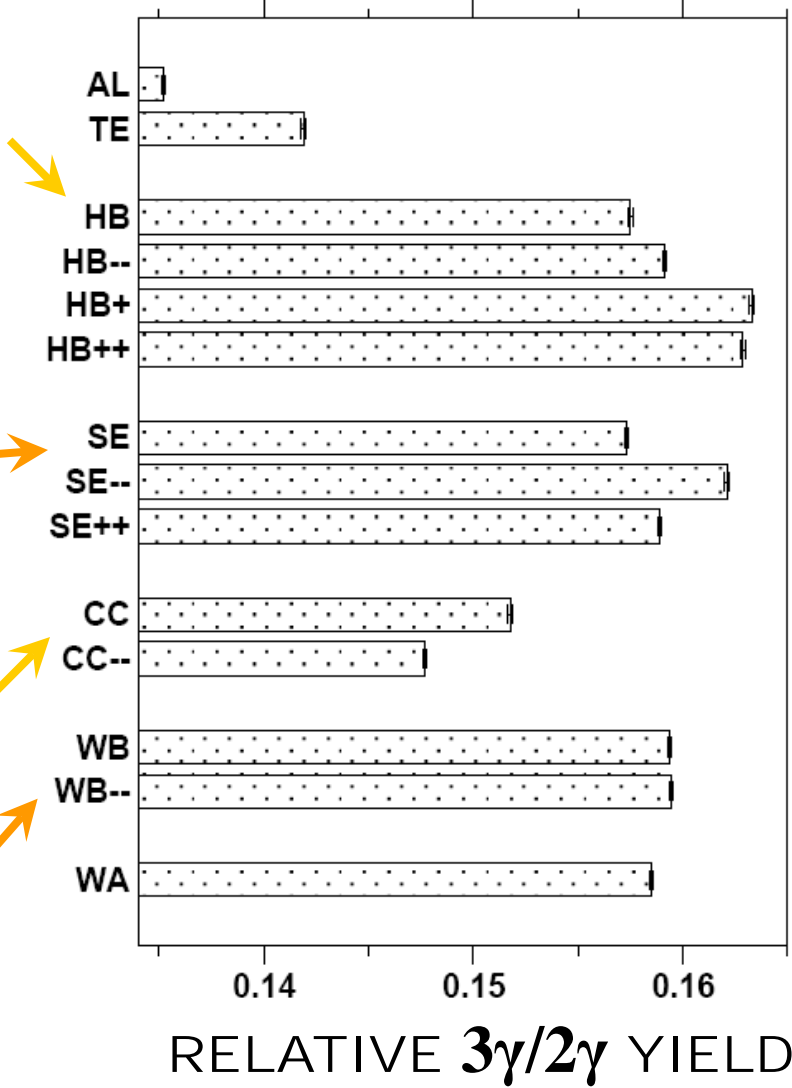
7	bgo_time	12 bit bgo time	(0x0fff)	0000 1111 1111 1111	[3]
8	bgo_low	12 bit bgo energy	(0x0fff)	0000 1111 1111 1111	[3]

HAEMOLYSED BBLOOD  
(HAEMOGLOBINS HAVE  
BEEN LIBERATED FROM  
RED BLOOD CELLS)

SERUM  
(LIKE PLASMA BUT NO  
CLOTTING FACTORS)

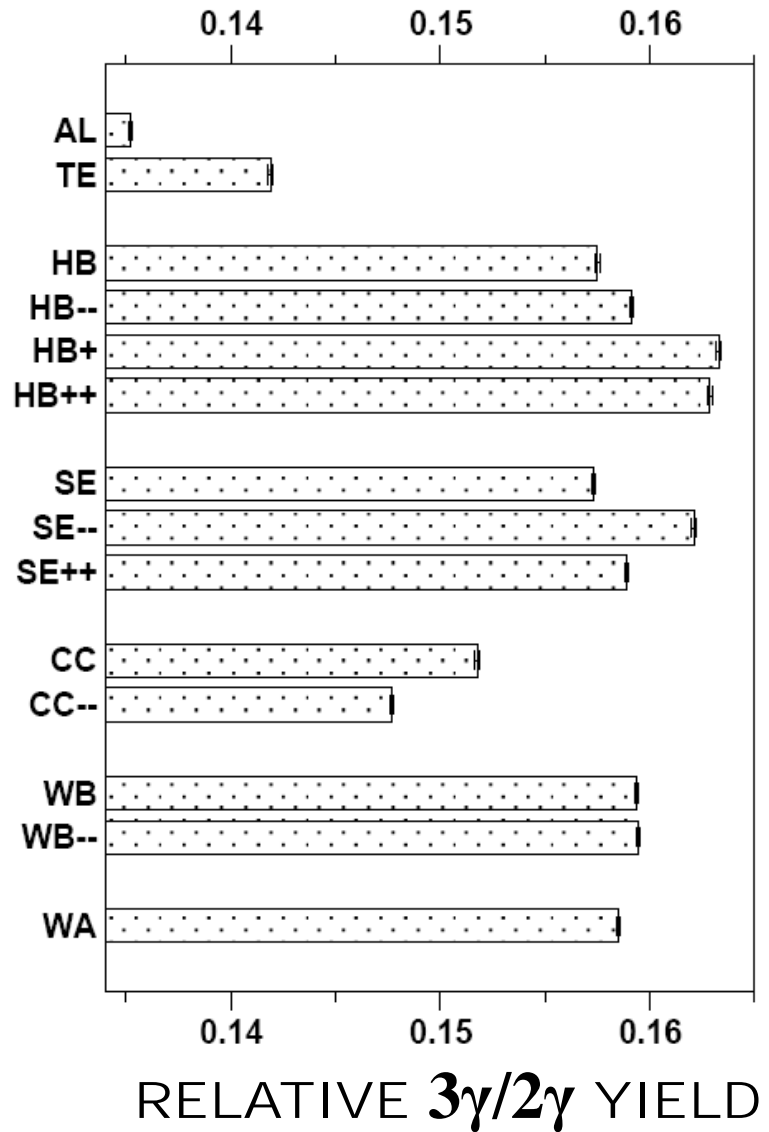
CELL CONCENTRATE  
(NO PLASMA)

WHOLE BBLOOD



THE FACT THAT  
THEY VARY IS  
ENCOURAGING –  
AT LEAST  
THE METHOD IS  
SENSITIVE TO  
*SOMETHING*

OXYGENATION IS NOT  
THE ONLY FACTOR.  
THERE ARE  
COMFOUNDING  
FACTORS PERTURBING  
THE 3-QUANTA YIELD



# THREE-QUANTAS STUDIES: DIFFICULTIES & CHALLENGES

## 1. PHYSICAL MEASUREMENT

- RARE EVENTS NOT EASY TO DETECT
- DIFFICULT TO PICK OUT FROM COMPTON-SCATTERED BACKGROUND (even with Compton-suppression)
- DEAD TIME

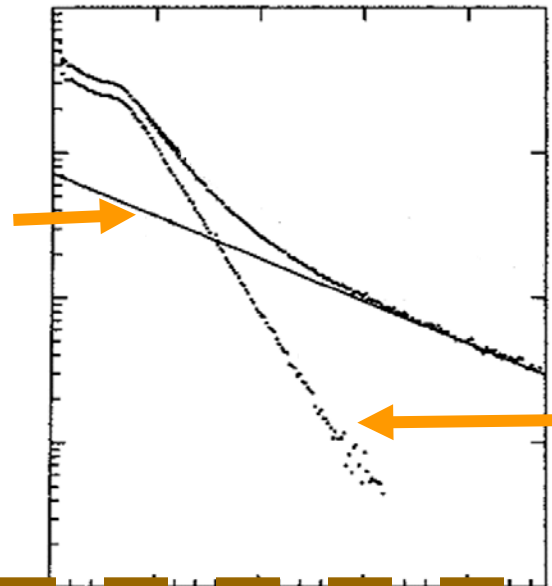
## 2. MONTE CARLO

- INTERACTION
- CROSS-SECTIONS
- CHEMICAL BINDING (same elemental composition bound/structured differently causes different 3-quanta yields  
– *THE SAME PROPERTY WHICH LENDS THE METHOD MOLECULAR IMAGING PROSPECTS*)

# DETECTION OF $3\gamma/2\gamma$ YIELDS

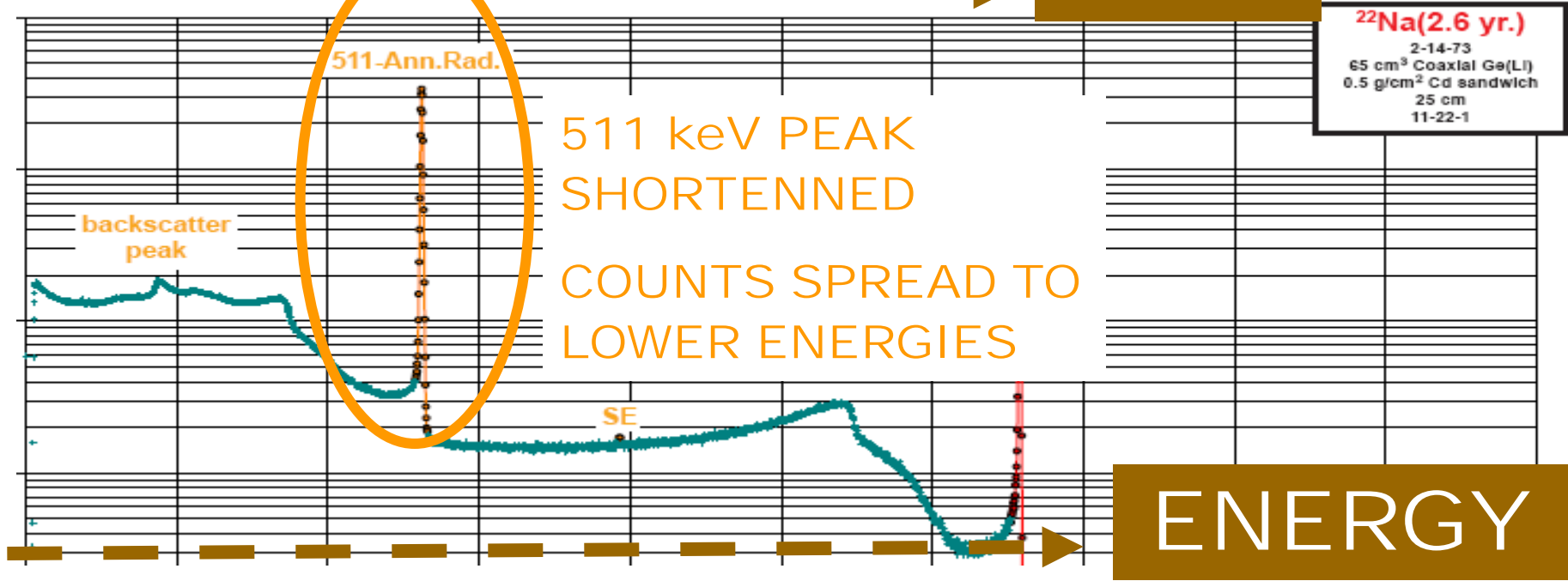
BESIDES TRIPLE  
COINCIDENCE

SLOW COMPONENT  
ORTHO-POSITRONIUMS  
( $3\gamma$ )



FAST COMPONENT  
FREE POSITRONS

TIME



Characteristic x-rays from bismuth

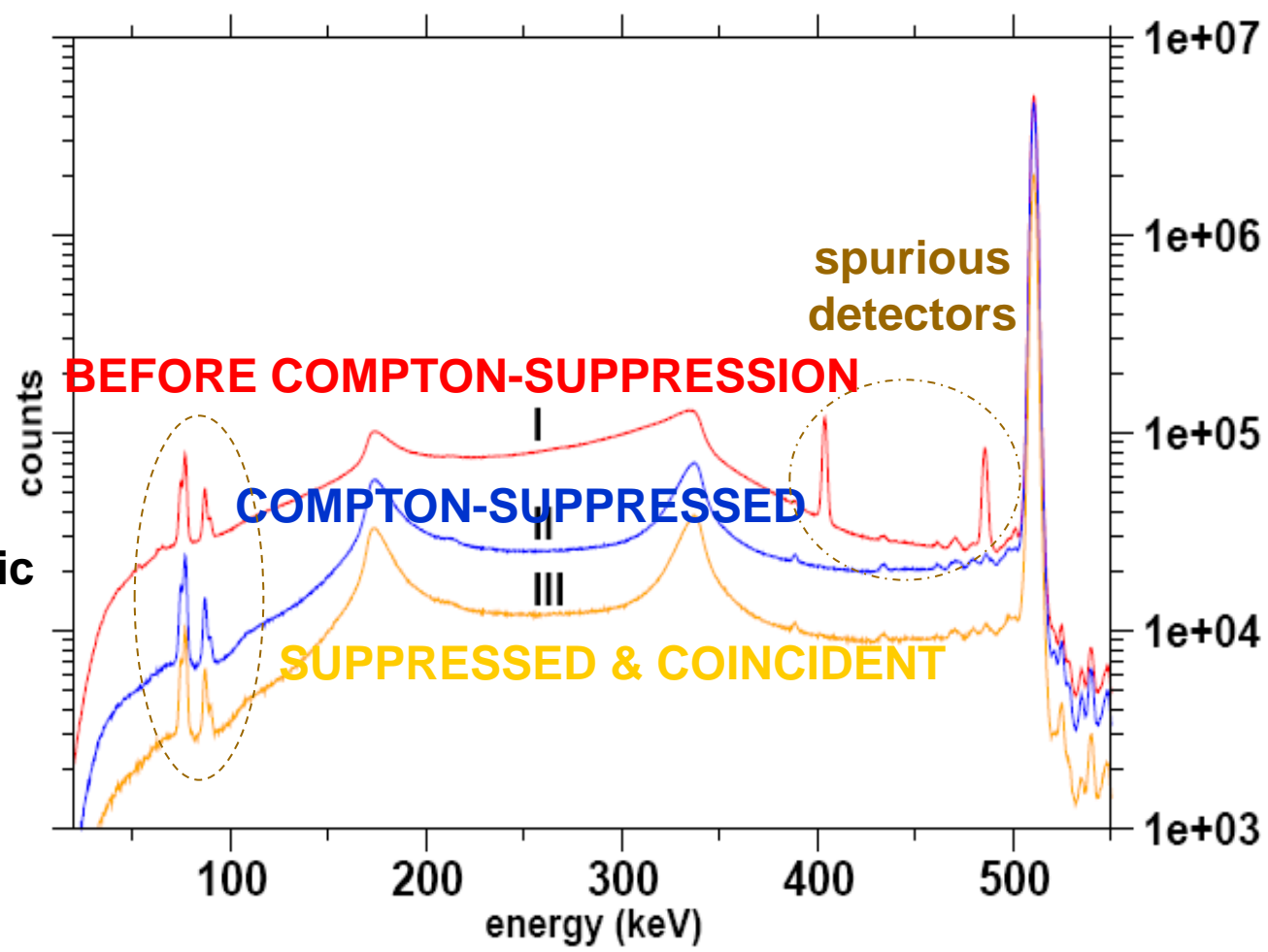
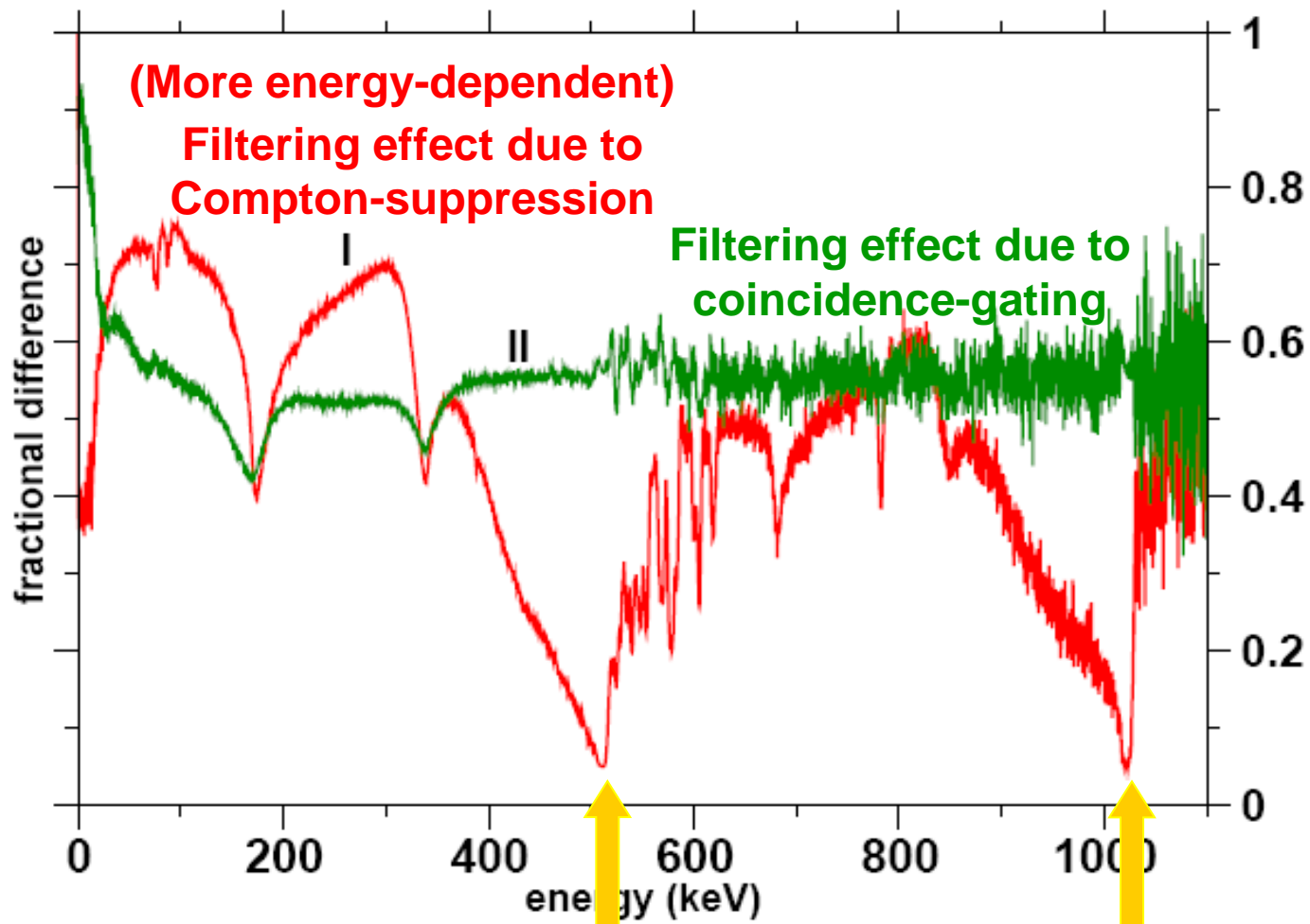


Fig. 1. Gamma spectra from the FDG source with the reference sample in place: (I) all hits from all detectors; (II) clean hits from non-outlying detectors only; (III) time-gated clean hits from non-outlying detectors only. The energy axis has been truncated.



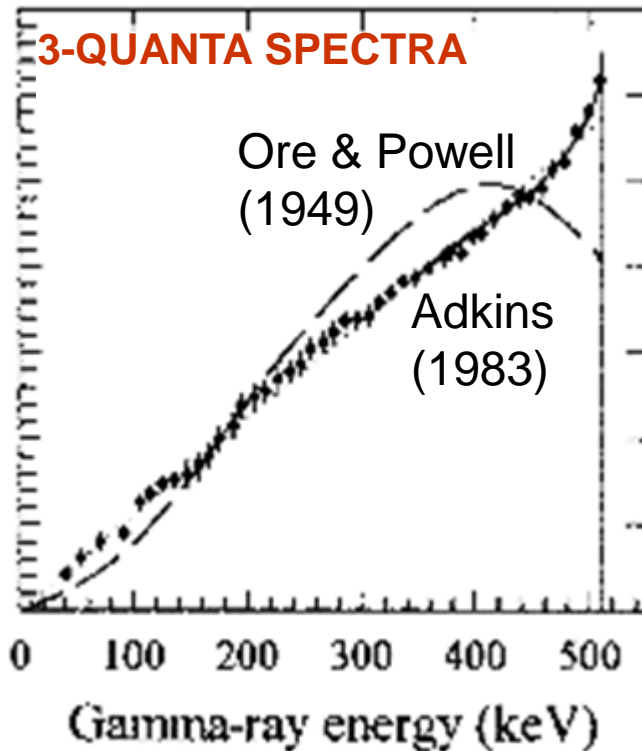
**FILTERED THE LEAST: FULL-ENERGY PHOTO-PEAK & SUMMED PEAK**

Fig. 2. Variation in filtering effects with energy: fractional difference in counts per energy bin (I) with and without Compton-suppression; (II) before and after time-gating.

# DIFFICULTIES & CHALLENGES

## STAGES OF FILTERING

1. COMPTON-SUPPRESSION
2. COINCIDENT TIME GATING
3. ANGULAR CORRELATION
4. ENERGY & MOMENTUM CONSERVATION



**IN OUR ATTEMPT TO CLEAN-UP  
THE SPECTRA TO SINGLE-OUT  
THREE-QUANTA COUNTS, WE  
INEVITABLY REMOVE THE  
COUNTS WE WANT, AND OBTAIN  
THE COUNTS WE DO NOT WANT**



## FURTHER WORK

TO SUPPRESS OR NOT TO SUPPRESS

FROM COMPTON-SUPPRESSION TO GAMMA-TRACKING

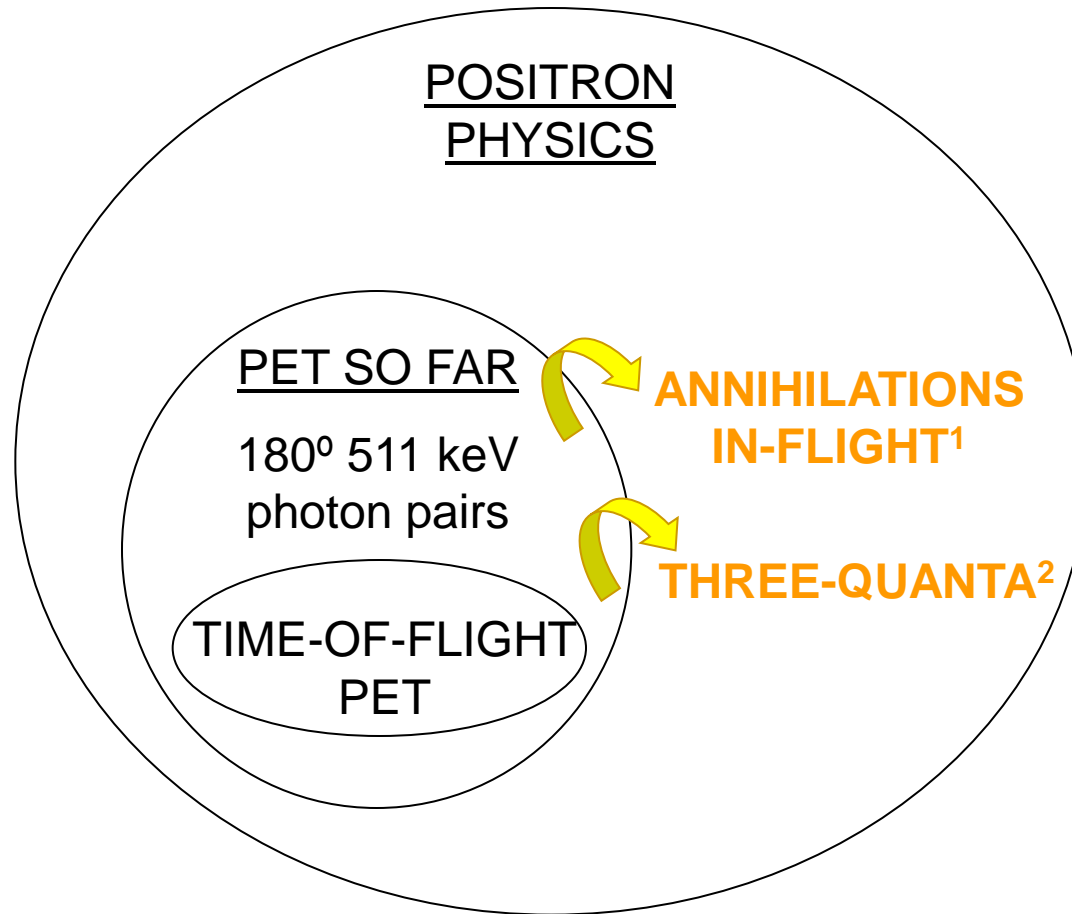
*To include Compton-scattered counts instead of removing them*

*Next-generation large-array detectors  
(AGATA and GRETA)*

*Great idea but is it going to work?*

# POSITRON EMISSION TOMOGRAPHY

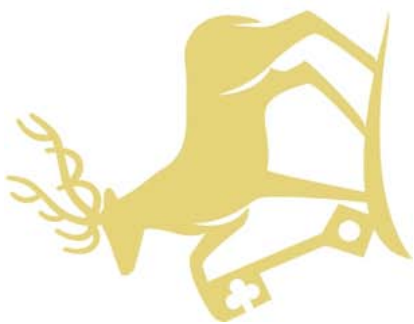
## NEEDS A RETHINK



Surrey's attempts in stepping out of the 'comfort zone':

<sup>1</sup> Chin & Spyrou 2007 NIM-A 580:481

<sup>2</sup> Latest work: this and Alkhorayef's presented in Cancun and Lisbon



Positron about to decay in flight	1	0.606	1	2	0.155,0.023,500.314	-0.122,-0.592, 0.797
Resulting photons	1	0.979	0	2	0.155,0.023 500.314	-0.311, 0.020, 0.950
	2	0.649	0	2	0.155,0.023 500.314	0.282,-0.935,-0.213

NOT 0.511      NOT BACK-TO-BACK!

